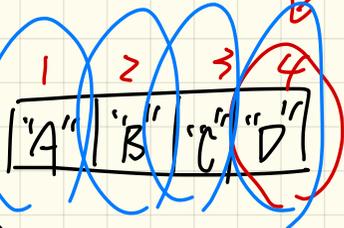


LECTURE 16
TUESDAY NOVEMBER 5

push

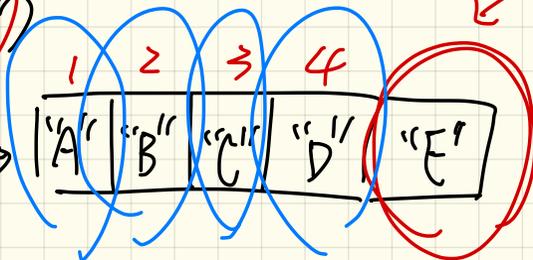
Str. I

old



push("E")

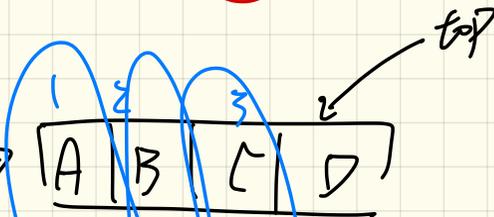
Current



pop

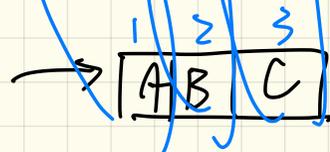
Str I

old



pop

Current



push

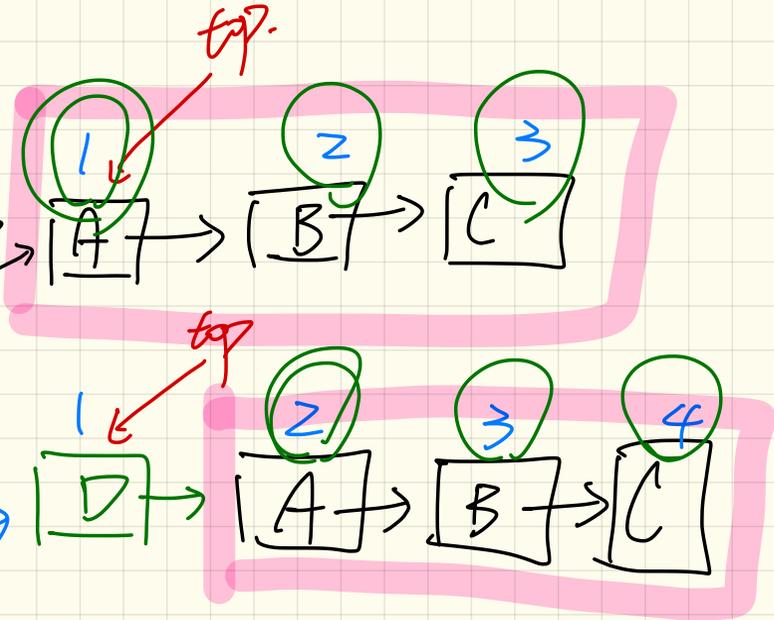
Str. 2

imp

old

push("D")

Current



Across 2 |..| Count is i

all
|
end

imp[i] ~ (old imp. d.t) [i-1]

Developing a LIFO Stack

SCP violated:

1. duplicates (contracts)

2. change on implementation may involve multiple changes on contracts

```
class LIFO_STACK[G] create make
feature {NONE} -- Strategy 1: array
imp: ARRAY[G]
feature -- Initialization
make do create imp.make_empty ensure imp.count = 0 end
feature -- Commands
push(g: G)
do imp.force(g, imp.count + 1)
ensure
  changed: imp.count ~ g
  unchanged: across 1 |..| count as i all
  imp[i.item] ~ (old imp.deep_twin)[i.item] end
end
pop
do imp.remove_tail(1)
ensure
  changed: count = old count - 1
  unchanged: across 1 |..| count as i all
  imp[i.item] ~ (old imp.deep_twin)[i.item] end
end
```

1. use a linked list when for 1st element to the top.

imp[i]

```
class LIFO_STACK[G] create make
feature {NONE} -- Strategy 2: linked-list first item as top
imp: LINKED_LIST[G]
feature -- Initialization
make do create imp.make ensure imp.count = 0 end
feature -- Commands
push(g: G)
do imp.put_front(g)
ensure
  changed: imp.first ~ g
  unchanged: across 2 |..| count as i all
  imp[i.item] ~ (old imp.deep_twin)[i.item - 1] end
end
pop
do imp.start ; imp.remove
ensure
  changed: count = old count - 1
  unchanged: across 1 |..| count as i all
  imp[i.item] ~ (old imp.deep_twin)[i.item + 1] end
end
```

```
class LIFO_STACK[G] create make
feature {NONE} -- Strategy 3: linked-list last item as top
imp: LINKED_LIST[G]
feature -- Initialization
make do create imp.make ensure imp.count = 0 end
feature -- Commands
push(g: G)
do imp.extend(g)
ensure
  changed: imp.last ~ g
  unchanged: across 1 |..| count - 1 as i all
  imp[i.item] ~ (old imp.deep_twin)[i.item] end
end
pop
do imp.finish ; imp.remove
ensure
  changed: count = old count - 1
  unchanged: across 1 |..| count as i all
  imp[i.item] ~ (old imp.deep_twin)[i.item] end
end
```

Using MATHMODELS Library

Implementing an Abstraction Function

```
class LIFO_STACK[G -> attached ANY] create make
feature {NONE} -- Implementation
imp: LINKED_LIST[G]
feature -- Abstraction function of the stack ADT
model: SEQ[G]
do create Result.make_empty
across imp as cursor loop Result.append(cursor.item) end
end
```

strategy 3

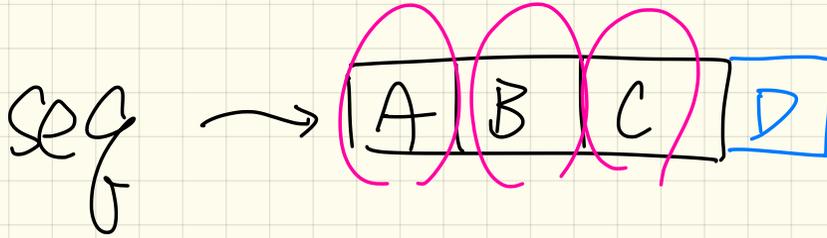
from MATHMODELS

LL

Writing Contracts using the Abstraction Function

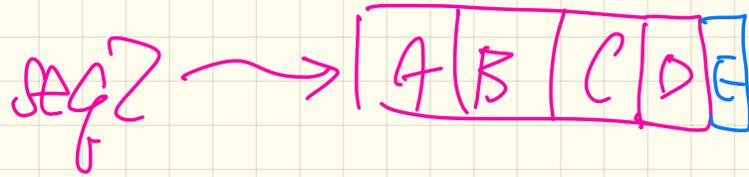
```
class LIFO_STACK[G -> attached ANY] create make
feature -- Abstraction function of the stack ADT
model: SEQ[G]
feature -- Commands
push (g: G)
ensure model ~ (old model.deep twin) appended(g) end
```

two separate calls to model.guez



seg.append(D)

↓ command.



seg := seg.appended(E)

↓ immutable seq.

MATH MODELS

1. Commands

↳ use to implement the
"mode" (e.g. append)

2. Immutable queries

↳ use to write contracts
(e.g. push)

Implementing a LIFO Stack



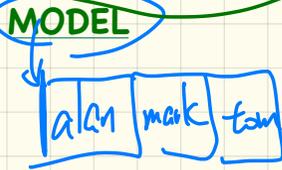
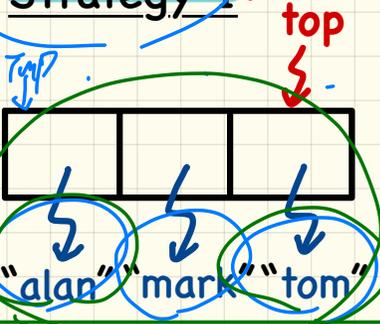
```

model: SEQ[G]
do
  across inp is q loop
  end ad Result. append(q)
  
```

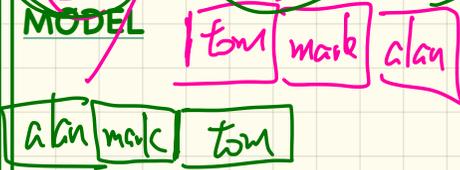
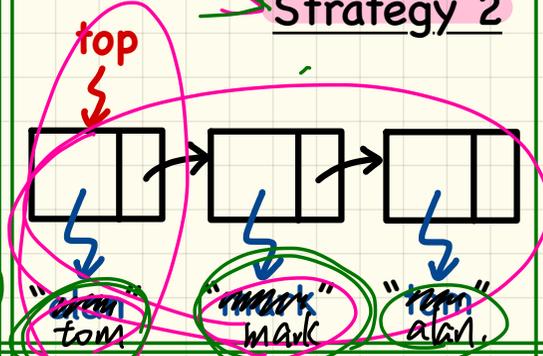
```

model: SEQ[G]
do
  across inp is q loop
  end ad Result. append(q)
  prepend
  
```

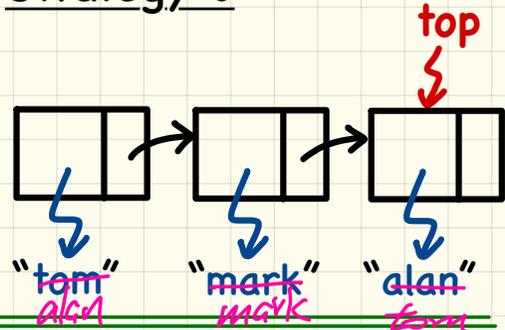
Strategy 1



Strategy 2

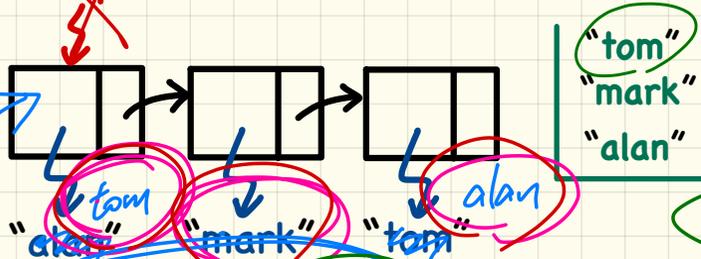


Strategy 3

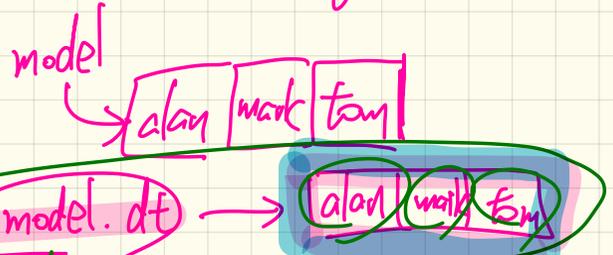


Pre-State

old IMPLEMENTATION



(keep prepending) **old MODEL**

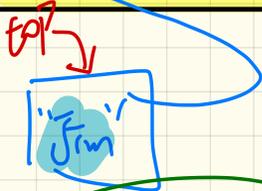


s.push("Jim")

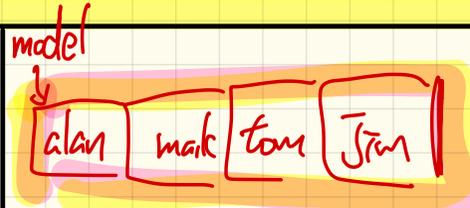
model.dt.appended(Jim) → [alan | mark | tom | Jim]

Post-State

IMPLEMENTATION



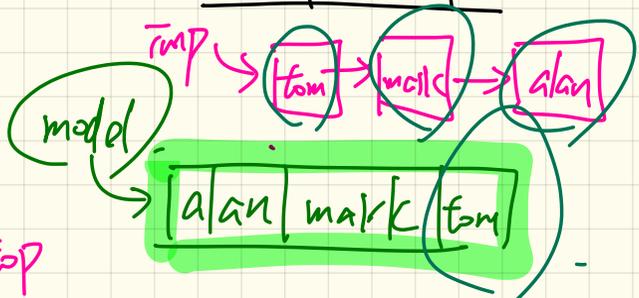
MODEL



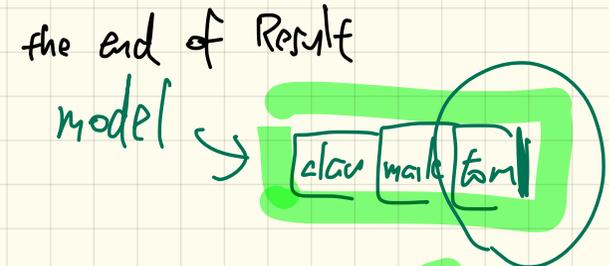
push (g: G)

ensure model ~ (old model.deep twin).appended (g) end

class STACK[G]
 feature {front}
 imp: ARRAY[G]
 LL[G]



feature
 public model: SEQ[G]
 do [keep appending to the end of Result
 prepending]
 top: $\frac{hd}{G}$
 ensure



Result ~ model.last

Strategy 1: Mathematical Abstraction

'push(g: G)' feature of LIFO_STACK ADT

public (client's view)

old model: SEQ[G]

model ~ (old model.deep_twin).appended(g)

model: SEQ[G]

abstraction function
convert the current array
into a math sequence

convert the current array
into a math sequence
abstraction function

old imp: ARRAY[G]

imp.force(g, imp.count + 1)

imp: ARRAY[G]

private/hidden (implementor's view)

Strategy 2: Mathematical Abstraction

'push(g: G)' feature of LIFO_STACK ADT

public (client's view)

old model: SEQ[G]

$\text{model} \sim (\text{old model}.\text{deep_twin}).\text{appended}(g)$

model: SEQ[G]

*abstraction
function*

*convert the current linked list
into a math sequence*

*convert the current linked list
into a math sequence*

*abstraction
function*

old imp: LINKED_LIST[G]

$\text{imp}.\text{put_front}(g)$

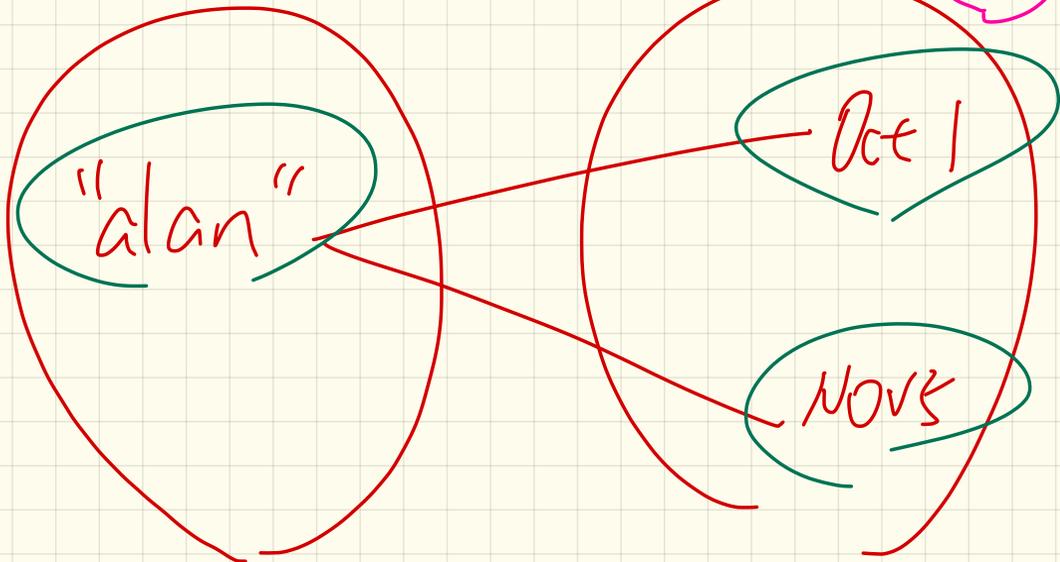
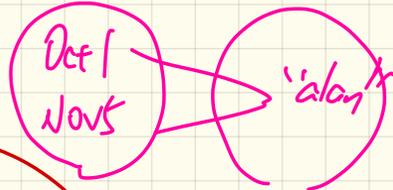
imp: LINKED_LIST[G]

private/hidden (implementor's view)

REL?

FUN? REL[DATE, NAME]

REL[NAME, DATE]



feature { NONE }

model: SEQ [G]

feature

get_model : SEQ [G]